Coded Excitation Plane Wave Imaging for Shear Wave Motion Detection

Pengfei Song, Member, IEEE, Matthew W. Urban, Senior Member, IEEE, Armando Manduca, Member, IEEE, James F. Greenleaf, Life Fellow, IEEE, and Shigao Chen, Member, IEEE

Abstract—Plane wave imaging has greatly advanced the field of shear wave elastography thanks to its ultrasonic imaging frame rate and the large field-of-view (FOV). However, plane wave imaging also has decreased penetration due to lack of transmit focusing, which makes it challenging to use plane waves for shear wave detection in deep tissues and in obese patients. This study investigated the feasibility of implementing coded excitation in plane wave imaging for shear wave detection, with the hypothesis that coded ultrasound signals can provide superior detection penetration and shear wave SNR compared with conventional ultrasound signals. Both phase encoding (Barker code) and frequency encoding (chirp code) methods were studied. A first phantom experiment showed an approximate penetration gain of 2 to 4 cm for the coded pulses. Two subsequent phantom studies showed that all coded pulses outperformed the conventional short imaging pulse by providing superior sensitivity to small motion and robustness to weak ultrasound signals. Finally, an in vivo liver case study on an obese subject (body mass index = 40) demonstrated the feasibility of using the proposed method for in vivo applications, and showed that all coded pulses could provide higher SNR shear wave signals than the conventional short pulse. These findings indicate that by using coded excitation shear wave detection, one can benefit from the ultrafast imaging frame rate and large FOV provided by plane wave imaging while preserving good penetration and shear wave signal quality, which is essential for obtaining robust shear elasticity measurements of tissue.

I. INTRODUCTION

Coded excitation has been applied to medical ultrasound imaging for more than two decades [1], [2]. Coded ultrasound signals possess superior penetration and SNR compared with conventional ultrasound signals, and have found many important applications such as B-mode imaging [2]–[8], synthetic aperture imaging [9], [10], color flow imaging [11]–[13], strain imaging [14], and acoustic radiation force impulse (ARFI) imaging [15]. Coded excitation enhances ultrasound signal SNR by elongating the duration of the ultrasound pulse so that more energy can be deposited into the tissue. This takes advantage of the fact that the thermal index of the conventional short imaging pulses is typically well below the regulatory limit by the Food and Drug Administration (FDA). The deteriorated range resolution caused by the long coded pulses can be recovered by the process of decoded filtering (or RF compression), which is typically done by correlating the received RF signal with the transmitted code [2], [16]. Recently, base-band compression has been introduced to improve compression efficiency [17], [18]. By careful design of the coding and decoding methods, one can achieve a robust imaging system with high SNR, good range resolution, and excellent penetration [1], [4], [5], [7].

The improved penetration and imaging SNR provided by coded ultrasound signals can be beneficial to shear wave motion detection, because the quality of the shear wave signal is closely related to the quality of the ultrasound signal [19]–[22]. For the last decade, the concept of using plane wave imaging for shear wave detection has greatly advanced the field of shear wave elastography, thanks to the ultrafast imaging frame rate and the large field-of-view (FOV) provided by plane waves [23]–[26]. The high imaging frame rate is essential to capture the fast propagating shear waves in stiff lesions such as breast cancer [27], and the large FOV is essential to perform large-volume sampling of tissues for applications such as liver fibrosis staging [28], [29]. The drawback of plane wave imaging, however, is the decreased penetration and low RF signal SNR due to the lack of transmit focusing, which makes it challenging to use plane waves to detect small tissue motions caused by shear waves in deep tissues and in obese patients. Although coherent spatial compounding has been proposed to significantly improve the SNR of plane waves [23], [30], the penetration of plane waves is still problematic due to lack of transmit focusing. The goal of this study, therefore, was to implement coded excitation in plane wave imaging for shear wave detection, with the hypothesis that shear wave signal SNR and shear wave detection penetration can be significantly improved by using coded ultrasound signals.

Both phase encoding and frequency encoding methods [1] were investigated in this study. Two representative codes were selected for each method: the Barker code for phase encoding and the linear frequency modulated (FM) chirp for frequency encoding. The Barker code is bi-phase and thus less demanding to the system transmitter than the chirp code. However, the longest length Barker code...
has a length of 13 bits, which limits its improvement of SNR and suppression of range side lobes [1]. Linear FM chirp, on the other hand, is not limited by length, but may suffer from degradation in range side lobes and also has higher hardware demands on the transmitters and the bandwidth of the transducers. Fortunately, the range side lobes can be reduced by mismatched filtering and envelope windowing of the transmitted chirp signal by the natural bandwidth of the ultrasound transducer [4], and one can also reduce the hardware demands by using the pseudo-chirp technique [2]. This paper, therefore, compares the performance of coded ultrasound signals for shear wave detection to conventional short ultrasound pulses, and also compares the performance of different coded signals.

This paper is structured as follows: in Section II, we introduce the relationship between ultrasound SNR and shear wave SNR, followed by experiment designs for evaluating the performance attributes of coded excitation for shear wave detection, including penetration, sensitivity to motion, and robustness to weak RF signal. In Section III, we first show two phantom studies (with and without a pork belly layer) to systematically compare the performance of coded excitation and conventional detection methods, followed by an in vivo liver case study to demonstrate the feasibility of using the proposed method for in vivo applications. We close the paper with discussion and conclusions.

II. MATERIALS AND METHODS

A. Ultrasound Signal SNR and Shear Wave Signal SNR

Shear wave motion signals are derived from ultrasound RF signals by a variety of methods [31]. Regardless of the differences among these methods, the shear wave motion signal SNR is related to the RF signal SNR, given by the Cramér-Rao lower bound proposed in [32] and [19]. Here we follow Walker and Trahey [19]:

$$\sigma(\Delta t - \hat{\Delta t}) \geq \sqrt{\frac{3}{2f_0^3\pi^2T\left(B^4 + 12B\right)}} \cdot \frac{\rho}{\sqrt{1 + \frac{1}{\text{SNR}_\text{RF}}}} - 1 \right) \right), \quad (1)$$

where $\sigma(\Delta t - \hat{\Delta t})$ is the standard deviation of the jitter error of shear wave motion detection (which is inversely proportional to the shear wave signal SNR), $f_0$ is the center frequency of the transmitted signal, $T$ is the window size used for motion calculation, $B$ is the fractional bandwidth, $\rho$ is the correlation coefficient between the RF signals used for motion calculation, and $\text{SNR}_\text{RF}$ is the SNR of the ultrasound signal. If assuming identical ultrasound center frequency, window size, fractional bandwidth, and a correlation coefficient of 1 (because minimal RF decorrelation is expected for shear wave imaging) for different imaging pulses, then (1) can be approximately reduced to

$$\text{SNR}_{\text{SW}} \propto \frac{1}{\sigma(\Delta t - \Delta \hat{t})} \leq \frac{1}{\sqrt{\left(1 + \frac{1}{\text{SNR}_\text{RF}}\right)^2 - 1}} \right). \quad (2)$$

where $\text{SNR}_{\text{SW}}$ is the shear wave motion SNR and is inversely proportional to the standard deviation of the jitter error. Eq. (2) can be used to approximately predict the outcome of shear wave signal SNR given different ultrasound signal SNR under the same shear wave generation setting.

B. Prediction of Shear Wave Signal SNR for the Coded Ultrasound Signals

Four imaging pulses were studied in this paper to form plane waves: a conventional short imaging pulse ($f_0 = 3$ MHz, pulse duration $\approx 0.33$ μs), a Barker code with length of 13 bits ($f_0 = 3$ MHz, pulse duration $\approx 4.36$ μs), a short linear FM pseudo-chirp pulse ($f_0$ from 2 to 4 MHz, pulse duration $\approx 4.49$ μs), and a long linear FM pseudo-chirp pulse with twice the duration of the short chirp pulse ($f_0$ from 2 MHz to 4 MHz, pulse duration $\approx 8.98$ μs). The short chirp pulse was designed to have the same duration as the Barker pulse, and the long chirp pulse was designed to investigate the advantage of the chirp pulses over Barker code in terms of longer code length. The coded pulses were programmed on a tri-state pulser of the Vantage ultrasound research system (Verasonics Inc., Redmond, WA, USA) [33]. A curved array transducer (C5–2v, Verasonics Inc.) was used throughout this study. The bandwidth of the transducer is 2 to 5 MHz. The transmitted waveforms from the C5–2v were measured in a water tank by a hydrophone (HGL-0200, Onda Corporation, Sunnyvale, CA, USA), and the frequency spectra were obtained using Fourier transform. The programmed code, transmitted waveforms, and corresponding spectra of the 4 pulses are shown in Fig. 1.

Fig. 1(e) shows that the chirp long pulse has the highest energy magnitude across the bandwidth of the C5–2v (2 to 5 MHz). The center frequency $f_0$ (given by the centroid of the spectrum) and fractional bandwidth $B$ (full-width at half-maximum divided by center frequency) are 2.73 MHz and 57.3% for the single pulse, 2.64 MHz and 65.5% for the Barker 13 pulse, 2.51 MHz and 57.9% for the chirp short pulse, and 2.53 MHz and 58.2% for the chirp long pulse. To predict the shear wave signal SNR of the 4 detection pulses, it is reasonable to assume that the 4 pulses have similar center frequency and bandwidth, and therefore (2) can be used. Because it is challenging to estimate the actual ultrasound noise level for the calculation of ultrasound SNR, it was assumed that the chirp long pulse has an SNR of 40 dB, so that the noise amplitude can be inversely estimated given the signal amplitude of the chirp long pulse. To estimate the signal amplitude of the chirp long pulse, the energy of the spectrum from 2 to 5 MHz [as shown in Fig. 1(e)] was summed. Then the noise amplitude was calculated by dividing the signal am-
amplitude by the assumed SNR of 40 dB. Note that 40 dB was an assumed SNR level for the purpose of convenient comparisons among different pulses and therefore can be replaced by any quantities or variables. This same noise amplitude was then used for all detection pulses to calculate ultrasound SNR. To study the behavior of shear wave SNR as a function of imaging depth, a 0.5 dB/cm/MHz attenuation coefficient was applied to the power spectrum of each detection pulse to estimate the ultrasound SNR and then the shear wave motion SNR at each depth. Fig. 2 shows the prediction of the behavior of the ultrasound SNR and shear wave motion SNR (in the form of standard
deviation of jitter error) as a function of depths. One can see that, theoretically, all the coded pulses would provide higher shear wave SNR than the conventional single pulse, and the chirp long pulse would outperform the Barker 13 pulse and the chirp short pulse. In shallow regions where ultrasound SNR is high, all pulses provide similar performance and the jitter error plateaus, which indicates that the shear wave SNR would plateau above certain ultrasound SNR. This agrees with the results shown in Walker and Trahey’s study [19].

C. RF Compression and Shear Wave Motion Calculation

The Vantage Verasonics system uses pixel-oriented software beamforming to beamform the RF signals that are collected in the channel data [34]. Before beamforming, the RF signal was compressed with decoding filters to recover range resolution. For the Barker 13 code, the spectrum inversion-based decoding filter [5] was used for the RF compression. For the chirp codes, matched filtering [4] was used instead of mismatched filtering because the transmitted chirp signals are already envelope-windowed by the natural bandwidth of the transducer, as shown in Figs. 1(c) and 1(d). Fig. 3 shows the B-mode images of a phantom (model 040GSE, CIRS Inc., Norfolk, VA, USA) obtained by using the 4 different detection pulses in the form of plane waves. One can see substantial improvement of B-mode imaging penetration from the coded pulses, as well as the preserved range resolution on the wires and cyst targets after RF compression. Fig. 4 shows the RF signals (before and after compression) of a thin wire submerged about 30 mm deep in the water from the 4 detect-
tion pulses. One can see that after compression, the main lobe widths of the coded pulses are comparable with that of the single pulse. The nonlinear propagation in water may have compromised the RF compression and resulted in deteriorated axial resolution (i.e., strong range lobes for the coded pulses). Nevertheless, the axial resolution for coded pulses was significantly improved after RF compression. The RF compressed channel data are beamformed and down-mixed to generate in-phase/quadrature (IQ) data. The IQ data of consecutive frames were then used to estimate axial particle velocity \( V_Z \) caused by shear wave propagation. The 1-D autocorrelation method [35] was used to calculate \( V_Z \).

D. Phantom Experiment I

To systematically study the performance of the 4 pulses for shear wave detection throughout a large range of depth, a loudspeaker setup was used to produce stable and controllable shear waves into a large phantom (model 040GSE, CIRS Inc.) with a dimension of \( 17.8 \times 12.7 \times 20.3 \text{ cm} \) (length \( \times \) width \( \times \) height). The loudspeaker setup is similar to the one used in a previous external vibration study [29]. Fig. 5 shows the schematic plot of the experiment setup. To obtain repeatable shear wave patterns, the loudspeaker was synchronized with the Vantage system by triggering, so that the Vantage system always started shear wave detection 200 ms after the vibration was started. The phantom was positioned on top of the loudspeaker. The positions of the phantom, loudspeaker, and ultrasound transducer did not change during these experiments. The total detection duration was 46 ms and the total vibration duration was 400 ms. A 50-Hz continuous vibration was used throughout the phantom study. For shear wave detection, the 4 detection pulses were transmitted in the form of plane waves at a pulse-repetition-frequency (PRF) of 2500 Hz. A 5-angle plane wave spatial compounding \((-9^\circ, -4.5^\circ, 0^\circ, 4.5^\circ, 9^\circ)\) was used to reduce speckle noise and improve ultrasound SNR [23], [30], which brings the effective PRF down to 500 Hz \((2500 \text{ Hz}/5 \text{ angles} = 500 \text{ Hz})\).

To analyze shear wave signal SNR, a Fourier transform was performed on the shear wave signal along the temporal direction for each imaging pixel. Fig. 6(a) shows a typical shear wave motion signal from a single pixel, and Fig. 6(b) shows the Fourier transform of the signal. In each spectrum at each pixel, as shown in Fig. 6(b), the signal energy at 50 Hz was considered as shear wave signal, and the rest of the spectrum was averaged and considered as shear wave detection noise. Shear wave motion SNR was then obtained by calculating the ratio of shear wave signal to the detection noise.

Fig. 7(a) shows a typical shear wave motion SNR map obtained using this method with the single pulse transmission. Variations of shear wave motion SNR can be observed inside the phantom (indicated by the region inside the red dashed lines), which are caused by inhomogeneous distributions of shear wave energy at different spatial locations due to standing waves. To measure shear wave motion SNR as a function of depth, a mean shear wave motion SNR was calculated by averaging the SNR values of all imaging pixels at the same depth. Fig. 7(b) shows the shear wave motion SNR-depth plot obtained using the map in Fig. 7(a) (first trial), as well as 4 more SNR-depth plots obtained from 4 other independent data acquisitions (trials 2 to 5). It can be seen that the shear wave pattern and shear wave motion SNR are very repeatable. As mentioned above, because the positions of the transducer, the phantom and the loudspeaker were fixed, it is feasible to use this proposed method to systematically compare the

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Fig. 4. Envelope signals (before and after compression) of a thin wire obtained from the 4 detection pulses.

Fig. 5. Schematic plot of the experiment setup.
shear wave detection performance of the 4 different detection pulses.

In the first part of the phantom experiment, the 0.5 dB/cm/MHz attenuation section of the CIRS 040GSE phantom was directly imaged by the C5–2v transducer with the 4 detection pulses, as shown in Fig. 5. Three experiments were designed:

1) To test penetration of shear wave detection, the same ultrasound transmit voltage [140 Vpp (peak-to-peak voltage)] and loudspeaker input voltage (800 mVpp) were used for all the detection pulses. One acquisition was taken for each detection pulse.

2) To test sensitivity to shear wave motion, the ultrasound transmit voltage was fixed at 140 Vpp for all detection pulses, and the loudspeaker input voltage was gradually turned down from 800 to 100 mVpp with a step size of 100 mVpp. One acquisition was taken for each detection pulse at each loudspeaker input voltage (32 data acquisitions in total). This experiment was designed to simulate an *in vivo* situation where shear wave motion is weak (i.e., poor shear wave generation) but RF signal is strong.

3) To test robustness to weak RF signal, the loudspeaker input voltage was fixed at 800 mVpp for all the detection pulses, and the ultrasound transmit voltage was gradually turned down from 140 to 10 Vpp with a step size of 20 Vpp from 140 to 20 Vpp, and a step size of 10 Vpp from 20 to 10 Vpp. One acquisition was taken for each detection pulse at each ultrasound transmit voltage (32 data acquisitions in total). This experiment was designed to simulate an *in vivo* situation where RF signal is weak (i.e., strong ultrasound attenuation) but shear wave motion is strong.

For each data acquisition, a 2-D shear wave motion SNR map and a SNR-depth plot similar to Fig. 7 were reconstructed.

**E. Phantom Experiment II**

To simulate *in vivo* imaging, a piece of excised pork belly (about 3 cm thick) was positioned between the transducer and phantom (Fig. 8), to introduce more attenuation and ultrasound reverberation clutter noise to shear wave detection. A thin layer of degassed water was poured between the pork belly and phantom surface to ensure good coupling. Steps 2) and 3) from the previous phantom study were repeated for this experiment setup.

Fig. 6. (a) Shear wave motion signal from a single pixel. (b) The Fourier transform of the signal in (a).

Fig. 7. (a) A typical shear wave motion SNR map obtained by the proposed experiment setup. The red dashed lines indicate the phantom region. (b) Plots of shear wave motion SNR versus depth from the 5 independent trials. The plots are almost all overlapping, demonstrating good repeatability of shear wave motion SNR measurement.
The 0.5 dB/cm/MHz attenuation section of the phantom was imaged. For each data acquisition, a 2-D shear wave SNR map and a SNR-depth plot similar to Fig. 7 were reconstructed.

F. In Vivo Liver Case Study

This part of the study was designed to compare in vivo performance of the coded ultrasound signals for shear wave detection. To achieve fair comparisons of the 4 detection pulses with identical imaging situations (e.g., similar FOV of the liver and similar shear wave motion inside the liver), the 4 detection pulses were programmed into one shear wave acquisition sequence. Upon triggering, the loudspeaker vibrated at 50 Hz continuously for 200 ms to reach a steady state of shear wave generation inside the liver. Then the Vantage system started shear wave detection (with the loudspeaker kept on) with the single pulse for 40 ms, followed by 40 ms of Barker 13 detection, 40 ms of chirp short detection, and 40 ms of chirp long detection. The entire data acquisition was done within 200 ms, which is short enough to assume that the liver inside the FOV was stationary given that the subject was also asked to hold their breath. Each detection pulse detects 2 cycles of the 50 Hz shear wave within the 40-ms window, therefore, the shear wave signal can be assumed to be identical for the 4 pulses. A real-time B-mode imaging sequence was programmed with the shear wave detection sequence for live B-mode guidance.

In this case study, a healthy volunteer with body mass index (BMI) of 40 was recruited. The study was approved by the Institutional Review Board of the Mayo Clinic and written consent was obtained from the subject. The ultrasound safety parameters (Table I) of all the detection pulses are all below FDA regulatory limits [36]. The mechanical index (MI) and thermal index (TI) were measured following the National Electrical Manufacturers Association (NEMA) standards [37]. The soft tissue thermal index for unscanned modes with aperture >1 cm² was used to calculate TI for all the shear wave detection pulses. The acoustic power was determined using hydrophone planar scanning methods. The duration of each detection pulse is calculated using a PRF of 2500 Hz and total detection duration of 40 ms (i.e., 100 firings). An effective shear wave imaging PRF of 1 Hz (i.e., one shear wave detection event per second) was assumed for the thermal model. To measure probe surface temperature rise (TR), a 30-gauge type T thermocouple (Omega Engineering Inc., Stamford, CT, USA) was sandwiched between the transducer and a piece of pork belly and five repeated measurements were taken for each detection pulse (five separate transmissions for the five measurements). The TR within the tissue was calculated using the following equation from Palmeri and Nightingale [38]:

$$\Delta T = \frac{2\alpha I}{c_v t},$$

where $\alpha$ is the ultrasound attenuation and was assumed to be 0.7 dB/cm/MHz to be conservative; $I$ is the $I_{SPTA}$ (spatial peak, pulse average intensity, non-derated to be conservative), $t$ is the time of the ultrasound transmission (40 ms), and $c_v$ is the heat capacity per unit volume (4.2 mWs/cm³/°C).

The subject was laid supine on the examination bed with the back coupled to the loudspeaker with right arm abducted [29]. A relatively large liver region free of major vessels was located. A total of 5 data acquisitions were obtained with 5 separate breath-holds. Similar to the processing method introduced in the phantom studies, shear wave SNR was calculated by taking the ratio of shear wave energy at 50 Hz to the detection noise. The average shear wave SNR from the 5 data acquisitions was used to compare the performance of the 4 detection pulses.

| TABLE I. SUMMARY OF MEASURED ULTRASOUND SAFETY PARAMETERS OF THE FOUR DETECTION PULSES. |
|---------------------------------------------|-------------|-------------|-------------|-------------|
| MI                                          | 0.44        | 0.47        | 0.54        | 0.61        |
| TI                                          | 0.01        | 0.04        | 0.08        | 0.16        |
| $I_{SPTA, 0.3}$ (mW/cm²) at 2500 Hz PRF     | 34.4        | 137.3       | 153.7       | 321.6       |
| TR (°C)                                     | <0.1        | <0.1        | <0.1        | 0.2         |
| Within tissue                               | 0.008       | 0.032       | 0.036       | 0.075       |
| FDA regulatory limit                        | 1.90        | 6           | 6           | 6           |
III. Results

A. Phantom Experiment I

Fig. 9 shows the shear wave SNR maps [Figs. 9(a) to 9(d)], snapshots of the shear wave motion at a time instant [Figs. 9(e) to 9(h)], and SNR-depth plots of the 4 detection pulses, with maximal ultrasound transmit voltage (140 Vpp) and loudspeaker input voltage (800 mVpp). One can clearly see the penetration gain of the coded pulses from the SNR maps and the shear wave motion plots: the coded pulses could all reach the bottom of the phantom, whereas the single pulse could not. The SNR-depth plot in Fig. 9(i) shows the details of the SNR behavior as a function of depth for the 4 pulses. One can see that the shear wave motion SNR of all coded pulses is higher than the single pulse beyond 4 cm of depth. The chirp long pulse shows the highest shear wave motion SNR beyond 10 cm of depth, followed by the chirp short pulse and the Barker 13 pulse. The SNR curves for different pulses merge together for depths shallower than 4 cm, which indicate a plateau of shear wave motion SNR when ultrasound SNR is above a certain threshold. These shear wave SNR results are in good agreement with the predicted SNR behavior shown in Fig. 2(b) in terms of the relative positions of the curves. If using a shear wave SNR cutoff of 15 dB, the gain in penetration of shear wave detection is approximately 2 cm for Barker 13, 3 cm for chirp short, and 4 cm for chirp long.

Fig. 10 shows the results of the second experiment, which was designed to test the sensitivity to shear wave motion of the 4 detection pulses. Figs. 10(a) to 10(d) show the shear wave SNR maps obtained from the minimal loudspeaker input voltage (100 mVpp). One can see that all coded pulses showed higher sensitivity to motion than the single pulse, with the chirp long pulse having the
highest sensitivity. It is interesting to see that given the same weak motion, the coded ultrasound signals could still detect the motion well, whereas the single pulse could not. This implies that in some in vivo shear wave imaging situations, the shear wave generation might actually be robust—it might be the compromised shear wave detection pulses that sometimes could not pick up the motion signal. Figs. 10(e) to 10(l) show the detailed shear wave SNR-depth plots obtained from all loudspeaker input voltages. All coded pulses show higher shear wave SNR than the conventional single pulse for all configurations. The chirp long pulse shows the highest sensitivity to motion, and both of the chirp pulses show better sensitivity to motion than the Barker 13 code for all the experiments, which are consistent with the theoretical predictions above. At the 100 mVpp input voltage, the single pulse suffered from weak shear wave motion and strong ultrasound attenuation. The shear wave SNR fell below 15 dB beyond 10 cm of depth. However, the chirp pulses could still detect robust shear wave signals with greater than 15 dB SNR until 15 cm depth, which is about a 5 cm gain of penetration as compared with the single pulse.

Fig. 11 shows the results of the third experiment, which was designed to test the robustness to weak RF signals of the 4 detection pulses. Figs. 11(a) to 11(d) show the shear wave SNR maps with minimal ultrasound transmit voltage (10 Vpp). Figs. 11(e) to 11(l) show the detailed SNR-depth plots of the 4 detection pulses with decreased ultrasound transmit voltage (from 140 to 10 Vpp). The decreased ultrasound transmit voltage was used to simulate weakened ultrasound RF signal. Again, as shown in Fig. 11, all coded pulses show significantly higher shear wave detection SNR and penetration than the single pulse. At 10 Vpp transmit voltage, the chirp long signal could still reach about 15 cm penetration, whereas the single pulse fell apart at about 8 cm. The chirp pulses, especially the chirp long pulse, had better performance than the Barker 13 pulse. These results indicate that in in vivo imaging situations where shear wave motion is strong but ultrasound attenuation is high (i.e., in obese patients), the coded pulses can substantially improve shear wave motion detection thanks to their high robustness to weak RF signals. It takes more ultrasound attenuation to severely deteriorate the shear wave signals detected by coded pulses than by conventional short pulses. Note that the ultrasound attenuation introduced here was simulated by decreasing the ultrasound transmit voltage, which does not include the effect of frequency dependent attenuation. Frequency dependent attenuation can compromise the performance of the coded pulses. This will be discussed later in the paper.

**B. Phantom Experiment II**

This part of the experiment added a piece of excised pork belly on top of the phantom to increase ultrasound attenuation and introduce reverberation clutter noise, and then repeated the tests shown in the previous section. The pork belly used in this study was mainly composed of fat, and the experiment was conducted at room temperature. Based on Goss et al. [39], the pig fat at 20°C has an ultrasound attenuation of 3.5 dB/cm/MHz, which should be a reasonable estimate of the attenuation of the pork belly used in this study. Fig. 12 shows the shear wave motion SNR maps (at minimal loudspeaker input volt-
Fig. 11. (a) to (d) Shear wave SNR maps of the 4 detection pulses at minimal ultrasound transmit voltage of 10 V. (e) to (l) Shear wave SNR-depth plots of the 4 detection pulses with gradually decreased ultrasound transmit voltage (140 to 10 V).

Fig. 12. Pork belly phantom study I. (a) to (d) Shear wave SNR maps of the 4 detection pulses at minimal loudspeaker input voltage of 100 mVpp. (e) to (l) Shear wave SNR-depth plots of the 4 detection pulses with gradually decreased input voltages (800 to 100 mVpp).
reverberation clutter noise introduced by the pork belly, as indicated by the good shear wave SNR beyond 3 cm of depth. However, inside the pork belly, the coded pulses give lower SNR at high ultrasound transmit voltage (Fig. 12), and the SNR gets much higher inside the pork belly at low ultrasound transmit voltage (Fig. 13). This may be caused by the strong reverberations of the long coded pulses inside the pork belly. Nevertheless, the shear wave detection did not seem to be affected by the reverberation beyond the pork belly region, and it is of less interest to obtain strong shear wave signals inside the subcutaneous fat and muscle tissue in vivo.

C. In Vivo Liver Case Study

Fig. 14(a) shows an example of the liver B-mode image from one of the five data acquisitions. A region of interest was manually selected to segment the liver for SNR analysis. Figs. 14(b) to 14(e) show shear wave SNR maps of the 4 detection pulses from one of the five data acquisitions. Figs. 14(f) to 14(i) show snapshots of the shear wave motion signal of the 4 detection pulses at the same time instant from one of the five data acquisitions. Fig. 14(j) shows the averaged SNR-depth plots from the 5 data acquisitions for the 4 detection pulses. These results indicate that all the coded pulses provide higher shear wave SNR than the single pulse, and the chirp long pulse provided the highest SNR. The first 9 cm of the SNR-depth plots are in good agreement with the phantom study results and the theoretical predictions shown above. Beyond 9 cm, all the SNR plots merged to a similarly high value. This was caused by the lower liver capsules that provide strong ultrasound reflections and thus strong RF signals, which would increase the shear wave SNR. Overall, from this challenging subject with high BMI, the shear wave motion SNR provided by the coded pulses are in general substantially higher than by the single pulse. The coded excitation technique enables strong penetration of the plane waves so that both high frame rate and large FOV (both width and depth) shear wave detection can be realized. Note that the FOV size in Fig. 14 was large enough to contain the entire liver, which is comparable with 2-D magnetic resonance elastography [40]. However, with the ultrafast frame rate provided by plane wave imaging, one can achieve much higher frame-rate shear wave imaging than magnetic resonance elastography.

IV. Discussion

This paper presents a systematic study of the feasibility of implementing coded excitation for shear wave detection with plane wave imaging, with the hypothesis that coded ultrasound signals can significantly improve shear wave detection penetration and shear wave signal SNR. The first phantom study demonstrated an approximate gain in penetration of 2, 3, and 4 cm for the Barker 13 pulse, the chirp short pulse, and the chirp long pulse, respectively, for shear wave motion detection. Both the phantom experiments with and without pork belly showed substantial gain in penetration and shear wave SNR for the coded pulses. All coded pulses demonstrated substan-
Theoretical vs. Experimental Results

The mismatch of the SNR curves between the theoretically predicted ones (e.g., Fig. 2) and the experiment results (e.g., Fig. 9) is primarily caused by the heterogeneous shear wave field. As mentioned above, synchronized triggering sequences and fixed positions of the probes, phantoms, and loudspeakers were used to obtain repeatable pattern of shear wave motions. The theory assumes a homogeneous shear wave motion field, but in reality it is very challenging to produce such a homogeneous shear wave motion field with equal shear wave amplitude throughout the phantom. Therefore, it is very challenging to obtain a uniform shear wave SNR map, and consequently the behavior of the shear wave SNR curves from experiments is affected by the shear wave pattern. Nev-

Fig. 14. (a) B-mode image of the liver and manually selected region of interest (ROI) for SNR calculation. (b) to (e) Shear wave SNR maps of the 4 detection pulses from one data acquisition. (f) to (i) Snapshots of the shear wave motion at the same time instant for the 4 detection pulses from one data acquisition. (j) SNR-depth plots of the 4 detection pulses. The SNR value for each pulse was averaged over the 5 independent data acquisitions.
The conventional single pulse used in this study was chosen in a way such that the center frequency and the bandwidth of the single pulse are similar to those of the coded pulses, as shown in Fig. 1(e). The main reason for doing this is to achieve similar conditions among the different pulses in terms of center frequency, bandwidth, etc., as indicated by (1), so that a convenient comparison among the different pulses could be achieved. In practice, to improve the SNR and penetration of the conventional single pulses for shear wave detection, one can either increase the pulse length, lower the center frequency, or add a band-pass filter to the RF signal to suppress out-of-band noise. Fig. 15 shows an example of the shear wave detection SNR performance of 3 conventional single pulses: 3-MHz center frequency with 1-cycle pulse length (the same one used in this study), 3-MHz center frequency with 4-cycle pulse length, and 2-MHz center frequency with 1-cycle pulse length. Also shown in Fig. 15 is the shear wave SNR from the band-pass filtered 3-MHz 4-cycle conventional pulse (band-pass filter center frequency = 3 MHz, bandwidth = 45%). The same setup used in this study was used to compare the three pulses with 140 Vpp transmission voltage and 800 mVpp vibration amplitude. From Fig. 15, one can see that all three pulses have similar shear wave SNR for less than about 11 cm depth, and then the 4-cycle 3MHz pulse gained slightly better penetration than the 1 cycle pulse, while the 2 MHz pulse gained significantly higher penetration than both of the 3-MHz pulses. Although the longer pulse length increases the total amount of energy deposited into the tissue, because the center frequency is still 3 MHz, this pulse still suffers from significant attenuation beyond a certain depth. From the shear wave SNR standpoint shown in (1), increased pulse length decreases the bandwidth of the pulse (i.e., the time bandwidth product remains constant), and therefore the shear wave SNR performance was not improved significantly [according to (1)]. For the 2-MHz pulse, attenuation was significantly less and therefore the penetration performance was improved. As compared with Fig. 9, however, the 2-MHz single pulse did not improve the SNR in shallower depth as the coded pulse did. One possible reason is that the time-bandwidth product of the 2-MHz single pulse is smaller than that of the coded pulses, and therefore the coded pulses outperformed the single pulse thanks to a higher ultrasound SNR provided by a higher time-bandwidth product. The band-pass filtered signal did not show significant improvement for shear wave detection as expected. One possible reason is that the ultrasound SNR for these uncoded conventional pulses has plateaued in the near field. Increasing the pulse duration or band-pass filtering the signal does not further increase the ultrasound SNR and shear wave SNR due to fixed time-bandwidth product. Another possible reason is that the experiment was conducted in a tissue-mimicking phantom with high echogenicity. The implementation of band-pass filter may be significant for in vivo applications with low ultrasound echo amplitude. The band-pass filtered signal had worse penetration than the unfiltered signal for depth >10 cm, possibly due to the removal of lower frequency component by the narrow band-pass filter.

The performance of the coded pulses can be further improved by designing decoding filters that account for frequency dependent attenuation [7]. Fig. 16 shows the spectrograms of the four detection pulses using a short-time Fourier transform on a single A-line. One can clearly see that the high frequency components of the pulses attenuate faster than the low frequency components. The decoding filters used in this study did not account for such frequency dependent attenuation. Therefore, the efficacy of RF compression could be compromised. In practice, it is challenging to adaptively design depth-dependent decoding filters because of unknown tissue attenuation. Future study is needed to investigate the impact of depth-dependent filtering on shear wave detection with coded excitation.

As briefly mentioned above, the proposed shear wave motion detection with coded excitation can be used for other shear wave sources as well such as acoustic radiation force and intrinsic physiological motion [41], [42]. As shown in Figs. 10 and 12, the coded pulses have higher sensitivity to shear wave motion than the short single pulse. The higher sensitivity is given by the higher ultrasound SNR of these coded pulses. In challenging tissues such as deep liver, kidney, and heart, the shear wave motion can be rather small. Using coded pulses can help better detect these motions. In less challenging tissues such as thyroid and breast where shear wave motion produced by acoustic radiation force is strong, one can potentially reduce the push beam intensity to reduce the shear wave amplitude because the coded pulses may still be able to robustly
detect these shear wave signals. The reduced push beam intensity can decrease the cooling period for the probe and tissue and potentially improve the shear wave imaging frame rate.

In this study, only plane wave imaging was investigated for shear wave detection with coded excitation. However, the same principle can be applied to other detection beams such as focused detection beams [43] and diverging beams [21], [44]. Also, this study only proposed the use of coded excitation for plane waves for shear wave detection. The same principles can be applied to other plane wave imaging applications such as ultrafast Doppler and functional ultrasound imaging [45]. Note that the same limitations and challenges of coded excitation in the context of medical ultrasound imaging, such as frequency-dependent attenuation in tissues, the time-bandwidth limitations imposed by medical ultrasound applications, and potential thermal issues, should also apply to these applications. One can optimize the coded excitation technique based on a specific application to best balance the tradeoffs.

The chirp long code showed better performance than the chirp short code and the Barker 13 code in this study, and both chirp codes showed better performance than the Barker 13 code. The codes were designed to achieve similar center frequency and bandwidth for the different pulses so that a simplified version of (1) could be used to predict the shear wave SNR. The chirp codes have stronger low-frequency content in the spectrum than the Barker 13 code, which may facilitate better penetration for the chirp codes. Meanwhile, the probe response to the Barker 13 code did not seem to be as good as the response to the chirp codes, as shown in Fig. 1. This may cause less efficient transmission of ultrasound energy for the Barker code and compromise its performance in shear wave detection. The chirp long code demonstrated the advantage of using chirp-coded excitation in terms of no code length limitations. However, one cannot use an extremely long chirp code due to the large near-field dead zone and possible waste of energy—it was shown that when ultrasound SNR is beyond a certain level, shear wave motion SNR plateaus. One can optimize the length of the chirp code based on different applications.

Plane wave imaging is usually not limited by MI due to the lack of transmit focusing. Increasing transmit voltage is an option for increasing plane wave imaging SNR, but the transmit voltage is limited by power supply and transducer elements breakdown voltage. With these limitations, the use of coded pulses becomes a viable solution to boost plane wave imaging SNR and shear wave signal SNR. Coded pulses may have thermal issues due to the long duration pulses, and therefore can be limited for real-time B-mode imaging. However, in the context of shear wave imaging where shear elasticity maps are refreshed once or twice per second, thermal issues are minimal and can be neglected, as shown in Table I.

The decoding processing time was about 12 s for all the coded pulses when using Matlab (The MathWorks Inc., Natick, MA, USA) scripts on an Intel Xeon 12-core 2.66-GHz computer. One can dramatically reduce the processing time by using GPU processing or other parallel processing tools. Fast decoding is necessary for real-time shear wave imaging.
There are some limitations of this study. First, the single pulse spectrum [i.e., the Fourier transform of Fig. 1(a) upper panel] extends from 0.7 to 3.9 MHz, and some of the low frequency components are outside the bandwidth of the probe (66.5% of energy is within the 2 to 5 MHz bandwidth of the probe). A dual-cycle single pulse would have fit the bandwidth of the transducer better (with 78.2% energy within the 2 to 5 MHz bandwidth of the probe) than the single-cycle pulse. Nevertheless, as shown in Fig. 15, the single-cycle 3-MHz pulse performed similarly to the elongated pulse. As discussed above, one possible reason is that the time-bandwidth product of uncoded pulses is constant and therefore ultrasound SNR does not improve with elongated pulses. Another possible reason is that the SNR of ultrasound echo is relatively high for shear wave imaging in tissues or phantoms as compared with echo from blood, thus limiting the benefit of longer pulse duration for single frequency pulses. Therefore, results obtained with the single cycle pulse in this study as a reference are still meaningful. Second, other phase encoding methods such as Golay codes were not studied. Golay codes do not have the length limitations of the Barker code and may achieve similar performance to the chirp codes. However, Golay codes require multiple transmit events, which may reduce motion detection PRF, and are also susceptible to physiological or gross motion. Third, Fig. 4 shows that the pulse compression performance was not optimal in this study. A few factors that may contribute to this are nonlinear propagation in water when creating the decoding filter, the use of a 3-level pulser, and suboptimal decoding filter design. Degraded pulse compression compromises the contrast of the coded pulses, which may be significant for certain shear wave elastography applications such as breast imaging where good contrast is critical for complex hypoechoic targets. Future studies are needed to optimize the decoding filters performance based on the 3-level pulser of the Vantage system and study the contrast performance of coded pulses both in vitro and in vivo. Finally, only a curved array was investigated in the study. Future study is needed to investigate linear array and phased array transducers for various shear wave applications.

V. Conclusions

This study investigated the feasibility of using coded excitation for shear wave detection, to increase the shear wave motion SNR and shear wave motion detection penetration for plane wave imaging. Both phantom results and the in vivo liver case study results demonstrated substantial improvement of shear wave motion SNR and detection penetration using the coded pulses as compared with the conventional short pulse. The coded pulses also showed significantly higher sensitivity to shear wave motion and robustness to weak RF signal compared with the conventional short pulse. The chirp pulses showed better performance than the Barker pulse, with the chirp long pulse demonstrating the best performance. These results are very promising for implementing coded excitation in shear wave detection for shear wave elastography, to facilitate robust shear elasticity measurements of tissue.

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sonic signal and image processing. Dr. Urban is a member of Eta Kappa Nu, Tau Beta Pi, the American Institute of Ultrasound in Medicine, IEEE, and the Acoustical Society of America.

Armando Manduca (M’89) received the Ph.D. degree in astronomy from the University of Maryland in 1980. He is a Professor of biomedical engineering and radiology and Chair of the Division of Biomedical Mathematics at the Mayo Clinic. His recent work has focused on the development of algorithms for the analysis of MR and ultrasound elastography data, image denoising, and compressed sensing reconstructions of MRI and CT data.

James F. Greenleaf (M’73–F’88–LM’08) received the B.S. degree in electrical engineering from the University of Utah, Salt Lake City, in 1964, the M.S. degree in engineering science from Purdue University, Lafayette, IN, in 1968, and the Ph.D. degree in engineering science from the Mayo Graduate School of Medicine, Rochester, MN, and Purdue University in 1970. He is currently Professor of Biomedical Engineering and Associate Professor of Medicine, Mayo Graduate School, and Consultant, Department of Physiology and Biomedical Engineering, and Internal Medicine, Division of Cardiovascular Diseases, Mayo Clinic Rochester. He has served on the IEEE Technical Committee for the Ultrasounds Symposium for ten years. He served on the IEEE Ultrasonics, Ferroelectrics, and Frequency Control Society (UFFC-S) Subcommittee on Ultrasonics in Medicine/IEEE Measurement Guide Editors, and on the IEEE Medical Ultrasound Committee. Dr. Greenleaf was President of the UFFC-S in 1992 and 1993.

Dr. Greenleaf has 18 patents and is recipient of the 1986 J. Holmes Pioneer Award and the 1998 William J. Fry Memorial Lecture Award from the American Institute of Ultrasound in Medicine and is a Fellow of IEEE, American Institute of Ultrasound in Medicine, and American Institute for Medical and Biological Engineering, and the Acoustical Society of America. Dr. Greenleaf was the Distinguished Lecturer for IEEE Ultrasonics, Ferroelectrics, and Frequency Control Society (1990–1991) and recipient of the Rayleigh Award (2004). His special field of interest is ultrasonic biomedical science, and he has published more than 450 articles and edited or authored five books in the field.

Shigao Chen (M’02) received B.S. and M.S. degrees in biomedical engineering from Tsinghua University, China, in 1995 and 1997, respectively, and the Ph.D. degree in biomedical imaging from the Mayo Graduate School, Rochester, MN, in 2002. He is currently an Associate Professor of the Mayo Clinic College of Medicine. His research interest is noninvasive quantification of the viscoelastic properties of soft tissue using ultrasound.